

H-1

cosmological principle: homogeneous, isotropic. true if $r > 100 \text{ Mpc}$

1) RW-metric: $ds^2 = c^2 dt^2 - a^2(t) \left[\frac{dr^2}{1 - k r^2} + r^2 d\Omega^2 \right]$

2) 1st Friedmann eqn: $\frac{\dot{a}^2}{a^2} + \frac{k c^2}{a^2} = \frac{8\pi G}{3} \rho$
derived from $E = T + V$ and $k \equiv -\frac{2E}{m a^2}$

3) 2nd Friedmann eqn: $\frac{\ddot{a}}{a} = -\frac{4\pi G}{3} (\rho + 3 \frac{P}{c^2})$
derived from time derivative of 1st and $dE + P dV = 0$ (adiabatic?)

4) $k = \begin{cases} -1 & \text{open} \\ 0 & \text{flat} \\ 1 & \text{closed} \end{cases}$ $\dot{a}$ cannot be zero $\rightarrow$ positive forever (1st FE)

2nd FE $\xrightarrow{P, \rho > 0}$ $\ddot{a}$ always negative

$\Rightarrow$ universe is expanding, but slower and slower

5) proper distance $d_p = a(t) \int_0^r \frac{dr}{\sqrt{1 - k r^2}} \Rightarrow \dot{d}_p = \frac{\dot{a}}{a} d_p$
(radial)

6) density parameter $\Omega = \frac{8\pi G \rho}{3H^2}$ as in 1st FE: $\frac{k c^2}{H^2 a^2} = \frac{8\pi G}{3H^2} \rho - 1$
Hubble's law with $H = \frac{\dot{a}}{a}$

critical density $\Omega_c = \frac{\rho}{\rho_c} \rightarrow$ then $k=0$

7) redshift z : $1+z = \frac{a(t_0)}{a(t)}$ derived from $[ds=0]$

8) deceleration parameter q : $q = -\frac{\ddot{a}}{a H^2} = -\frac{\ddot{a} a}{\dot{a}^2}$

9) Always: $\rho \sim \frac{1}{a^2}$

matter dominated: $\begin{cases} \rho \sim a^{-3} \\ P=0 \end{cases}$
radiation: $\begin{cases} \rho \sim a^{-4} \\ P = \rho/3 \end{cases}$
derived from $\begin{cases} dU + P dV = 0 \\ U = \rho V \sim \rho a^3 \end{cases}$
 $\begin{cases} a \sim t^{2/3} \\ a \sim t^{1/2} \end{cases}$

10) age of universe: $t(z) = \frac{1}{H_0} \int_0^{1+z} \frac{1}{\sqrt{(1-\Omega_0) + \Omega_0/x}}$ with $x = \frac{a}{a_0}$ (2)
 derived from general 1st FE ($\propto a^2$ and $\propto a^2$; $\rho = \rho_0 \frac{a^3}{a_0^3}$)
 $\Rightarrow$ ~~$t(z)$~~ $t(0) = \frac{2}{3H_0}$

11) Einstein eqn with cosmological Λ :

$$G_{\mu\nu} - \Lambda g_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}$$

$\Rightarrow$ 2nd FE shows now that Λ is an accelerating term.
 $\rightarrow$ longer age of universe

~~11b)~~ $\rho \mapsto \rho + \rho_\Lambda$ with $\rho_\Lambda = \frac{\Lambda c^2}{8\pi G}$

$\Rightarrow$ negative pressure!
 $\rho_\Lambda = -3P_\Lambda \leftarrow$ 2nd FE

12) flatness condition (with $\Omega_\Lambda = \frac{\Lambda c^2}{3H^2}$): $\Omega + \Omega_\Lambda = 1$

H2

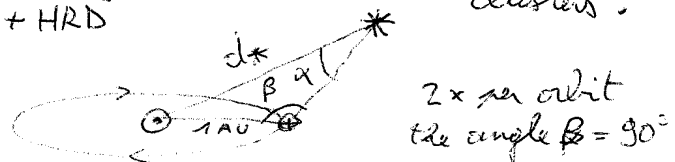
13) Hubble law: $v = Hd$

Correction: intrinsic v_{peculiar} component as large as 500 km/s

14) Distance ladder ($v = H_0 d$: 1 is easy, now find d)
 to calculate H_0

* also: fundamental plane for elliptical galaxies		Type Ia - SN: white dwarf accretes matter and explodes at M_{Chandra} with high L and very homogeneous (no metal dependence). But: $M < M_{\text{Ch}}$ may happen depending on explosion location and accretion speed.
		planetary nebulae: relatively homogeneous in terms of mass and L
		pulsating stars: independent of cause of instability; longer and more diluted stars have longer periods.
		Cepheids: small T-range for given L : period-density rel. + mass- L rel. = period-luminosity rel.
		HRD + distance modulus relating $(d, m_x, M_x) \rightarrow$ good for clusters! get M_x from observed spectrum + HRD

parallax: $\sin \alpha = \frac{1 \text{ AU}}{d^*}$
 1 AU



2x per orbit the angle $\beta = 90^\circ$

Bonus: secondary distance indicators, like Tully-Fischer relation, relating L and v_{rot} *

15) cosmochronology: compare abundances of unstable and stable isotopes. $\rightarrow$ age of universe (3)

16) age determination from clusters:

* specific HRD: age determination e.g. by MS cutoff point.

* if no heavy metals: $t_{\text{cluster}} \rightarrow t_{\text{universe}}$ (1st gen stars)

rotation neglectation may underestimate t_{uni} (rotation $\rightarrow$ mix core with shell $\rightarrow$ extend MS period)

17) proper distance expansion: $d_p = a_0 r = \frac{c}{H_0} \left(z - \frac{1}{2}(1+q_0)z^2 + \dots \right)$

depends on history of universe, and

1) photons are redshifted

2) photon packets smeared out in time $\Rightarrow$ factor $\left(\frac{a}{a_0}\right)^2 \Rightarrow L \sim \frac{1}{r^2} \Rightarrow \frac{a^2}{a_0^2 r^2}$

$\Rightarrow d \sim r \Rightarrow \frac{a_0}{a}$

so, $d_L = \frac{a_0}{a} d_p$ (luminosity distance)

18) deceleration parameter $q_0 \sim$ deviation from linear Hubble law $\rightarrow$ need high z measurements. q_0 seems small.

19) to determine Ω we need to estimate matter components at scales $> 100 \text{ Mpc}$ (cosmological principle). Pitfalls:

1) $L \sim M^4$ but IMF $\Phi(M) \sim M^{-2.35}$

$\rightarrow$ possibly infinite # low mass objects?

brown dwarf cutoff + brown dwarfing stars NO.

2) determination of M cannot rely on optical alone: 1/3rd of M in spiral galaxy is in the ISM.

3) dark matter

4) unclear how much gas remains in IGM after galaxy formation

But: upper limit for $\Omega_{\text{baryon}} = 3\%$ set by He-abundance (see H3)

20) $\frac{d}{dz} \rightarrow H_0, q_0$ ($\frac{c}{H_0}$ is slope of $d_p(z)$)

rel. abundance, clusters $\rightarrow$ ages

density $\rightarrow \Omega = \rho/\rho_c$

CMB $\rightarrow T_0, C_{\text{radiation}}$

early nucleosynthesis $\rightarrow \Omega_{\text{baryon}}$

21) dark matter proof:

(4)

- 1) peculiar (=intrinsic) velocities of galaxies higher than expected by gravity on basis of ~~present~~ mass.
(Zwicky)
(virial mass) The cluster could be in non-equil, but it doesn't seem to evolve ^{visible}
- 2) $\rho \nabla \Phi = -\nabla \rho$ the pressure gradient measured, corresponds to higher ~~than~~ gravitating mass than observed.
(X-rays)
- 3) spiral galaxies (spiral traces star formation) would not conserve ~~spiral~~ character with so few mass in outer rims ($\rightarrow$ dark matter halo)
- 4) spiral galaxies' rotation speed curves fall off as $r^{-1/2}$.
(galaxy laws) However, at the edge higher rotation speeds are detected: possible with d.m. halo.

Bonus: the unseen matter really is non-baryonic; otherwise nucleosynthesis ~~the~~ results would have been different than observed and predicted.

22) CMB characteristics:

- 1) isotropic $\rightarrow$ CMB comes from universe itself.
- 2) intense $\leftarrow$ spread out across whole sky
 $\rightarrow$ must be the whole universe itself.
- 3) blackbody spectrum. with $T \approx 2.7\text{ K}$
since $\rho \sim T^4$ for a BB and also $\rho_{\text{rad}} \sim a^{-4}$
we have $T \sim a^{-1}$.

$\hookrightarrow$ proof: clear absorption lines corresponding to CMB spectrum at higher T. in an ISM spectrum at high z

Bonus: contains: multipole anisotropy (very small: fluctuations)
dipole (Doppler shift) (600 km/s)
foreground (visible objects in sky)

23] Hubble law $\Rightarrow$ expanding universe

But: RW metric $\Rightarrow$ Hubble law
and cosmological principle $\Rightarrow$ RW metric

So: cosmological principle $\Rightarrow$ expanding universe

24] To understand the universe's evolution, we need not know it's history; just like thermodynamical equilibrium allows us to ascribe properties to a system

25] Early history of universe is one of phase transitions. Different eras:

1) hadronic era: $t < 10^{-4} s$; $T > 10^{12} K$
hadron-antihadron pairs; inflation.

2) leptonic era: $10^{-4} s < t < 1 s$; $10^{12} K > T > 10^{10} K$
electron-positron pairs; neutrinos decouple
at the end $\Rightarrow$ no more β -decay
 $\Rightarrow \frac{n_n}{n_p}$ frozen in at 0.17

3) radiation era: $1 s < t < ?$; $10^{10} K > T > 10^4 K$
 $E_{rad} \gg E_m$
 $\downarrow$
 $t \approx 1500$
first 3 minutes: nucleosynthesis, but all is still ionised.
 $E_m: 12 g/l \rightarrow 10^{-20} g/l$ and thus
(Thomson scattering) mean free path of radiation
from $\sim 1 cm \rightarrow \sim 2 pc$. Still "small"
 $\rightarrow$ "BB radiation"

4) matter era: $t ?$; $10^4 K > T$

Hydrogen in increasingly neutral state.
 $\rightarrow$ (until $T = 10^3 K$) recombination epoch
from $10^3 K > T$: decoupling epoch:
all H is neutral.

(inner and outer surface of last scattering)

After decoupling there's barely any radiation pressure
 $\rightarrow$ gravity starts shaping the universe

26] chemical evolution of a galaxy:

1st gen stons contain no ~~heavy~~ heavy elements.

G - dwarf problem: no α metallicity star is known.

Though He is produced ~~also~~ in stars, like heavy elements, its relative abundance is very high (26% He, 72% H, 2% metals) so 24% He needs another explanation $\rightarrow$ primordial nucleosynthesis

27] explaining relative abundances of heavy metals:

- 1) most are α -elements, others are products of secondary reactions
- 2) beyond iron: explosive nucleosynthesis from core-collapse SN

via n -process

人

rapid no capture

 p^+ capture

slow n° capture

- 3) iron peak: mostly Ia SN where the explosion is thermonuclear.

28 After leptonic era, $\frac{n^0}{n_p}$ frozen out at 0.17, but T was not yet low enough for nucleosynthesis and $\tau_n \approx 10 \text{ min.}$
 $\rightarrow \frac{n^0}{n_p}$ fell back to $1/7 \approx 0.14$

24) $n + p \rightarrow {}^2\text{H} + \gamma$
and other reactions $\rightarrow {}^4\text{He}$ } primordial nucleosynthesis

All neutrons are soaked up into ^4He nuclei;

rel. mass fraction $(1/7 + 1/7) / (1 - 1/7) \approx 0.25$ which explains
No higher elements yet because of unstable ${}^9\text{Be}$. the extra 24%

30) Though, the amount of "He formed" depends on e .

Also, tiny bits of ${}^7\text{Li}$ can be made if ρ is high enough,

$\rho_{crit, uni} \approx 10^{-30} \text{ g/cm}^3$

low ρ : ${}^4\text{He} + {}^3\text{H} \rightarrow {}^7\text{Li}$

↳ high p : $e^- + {}^4\text{He} + {}^3\text{He} \rightarrow e^- + {}^7\text{Be} \rightarrow {}^7\text{Li}$ dominates.

which explains the sudden rise in fig 3-1 p 53.

31 Observed He - abundance is strongest evidence of ~~BB~~ big bang primordial nucleosynthesis.

But: hard to constrain:

- 1) old stars are too cool and have no He - absorption lines
- 2) hot old stars have evolved too far and have more than

→ globular clusters: compare HRD with theoretical isochrones ^{own}

32) But there are 3 better methods to obtain primordial ~~He~~ abundances:

- 1) He-absorption lines in ISM (HII-regions, near young massive stars)
The He-abundance there scales with ^{16}O -abundance and can be extrapolated towards zero ^{16}O -content.
- 2) ^3H -abundances in the ISM by shifted absorption spectra (best for Hydrogen)
But: Stark broadening makes for inaccuracies.
- 3) ^7Li : has a strong resonance in the visible band.
 ^7Li is easily destroyed by mixing and thus disappears in metal-rich stars.
For old stars (spanning 2 orders of magn. in metallicity) a constant abundance is found (Spite plateau)
→ unmixed stars → primordial value.
But: value found is quite low. Need gravitational diffusion.

33) BB-model issues:

- 1) flatness problem: $\Omega_0 \approx 10^{-5}$ so at nucleosynthesis $\Omega \sim 10^{-13}$ which seems an odd coincidence.
- 2) horizon problem: CMB at same temperature everywhere, even though points had no causal contact.
Horizon distance $d_H = 3ct$ (matter dom.)
Hubble $2ct$ (rad. dom.)
derived from definition and $ds = 0$ (RW)
- 3) monopole problem: phase transitions should produce relic particles (with mass) though still the universe was dominated by radiation.

34) inflation: suppose $\dot{a} \gg 0$ temporarily.

($P < -e/3$) 1st FE now implies a negative P_{neg} because strong energy condition $e + P > 0$ is abandoned.

Through $T_{00} = 0$ this implies $P_{\text{vac}} = -e c^2$, so the

1st FE becomes $\frac{\ddot{a}}{a} = \frac{3\pi G}{3} \rho \Rightarrow a(t) \sim \exp\left[\left(\frac{8\pi G}{3}\right)^{1/2} t\right]$

- 35 | inflation solves the BB-problems: (8)
- 1) inflation washed out deviations from $\Omega = 1$ because 1st FE: $\Omega \approx 1 + \sim \frac{1}{a}$
 - 2) inflation ~~allows~~ allows the local universe ~~to~~ to expand more rapidly than ~~C~~ ~~the rest of the universe~~

Bonus: inflation models can be adapted for a nonzero Λ

36 | slow-roll inflation by scalar field ϕ inflaton φ .
with energy tensor of perfect fluid:

$$\begin{cases} \rho = \frac{1}{2} \dot{\varphi}^2 + V(\varphi) \\ p = \frac{1}{2} \dot{\varphi}^2 - V(\varphi) \end{cases} \Rightarrow \dot{\varphi}^2 < V(\varphi) \quad p < -\rho/3$$

moreover, if $\dot{\varphi}^2 \ll V(\varphi)$, then $a(t) \sim e^{Ht}$

Slow-roll requires $V(\varphi)$ to be flat. ~~After~~ When that ends the inflaton energy converts to massive particles (and radiation)

37 | Density perturbations in early universe have a QM origin, and wavevectors have Gaussian distrib.
Power ~~spectrum~~ spectrum: $\delta_{\varphi}^2(k) = \frac{k^3 \sigma_{\varphi}^2}{2\pi^2}$
 $f(\vec{x}) = \int \frac{d^3k}{(2\pi)^{3/2}} f_k e^{i\vec{k} \cdot \vec{x}}$

38 | inflationary perturbations are nearly scale-invariant (i.e. independent of k):

$$\sigma_k^2 = \left(H^2 \tau^2 + \frac{H^2}{k^2} \right) \approx \frac{H^2}{2k^3}, \text{ so } \delta_{\varphi}^2(k) = \frac{H^2}{4k^2}$$

This is because the integral of the power spectrum will mainly get contributions from small k , because high k 's cancel each other out.

39 | vacuum energy corresponds to a cosmological const.
Cosmological constant: quantum corrections to its value are an order of magnitude larger than what is observed. Perhaps slow-roll inflation (which mimics vacuum energy) is a solution?

40] gravitational instability: in a contracting cloud there is no immediate rise in P or T : radiation cooling prevents significant T increase at low ρ (isothermal)

41] Jeans criterion for isothermal perturbations to the e.o.m, e.o.s, Poisson's & mass continuity eqn; and assuming solutions proportional to $\exp(i(kx + \omega t))$:
 $\lambda > \left(\frac{\pi}{G\rho}\right)^{1/2} c_s = \lambda_J$ with dispersion relation $\omega^2 = k^2 c_s^2 - 4\pi G \rho$
 and $k = \frac{2\pi}{\lambda}$

Jeans mass (contained in a sphere with radius $\frac{\lambda_J}{2}$):

$$M_J = \frac{\pi}{6} \rho \lambda_J^3 \sim \rho^{3/2} \rho^{-2}$$

42] In the case of an expanding universe (ρ and v not const) and assuming Fourier expansion solutions with time dependent coefficients, one finds a power dependence of the perturbations on time rather than exponential; with a decaying adiabatic mode $\sim t^{-1}$ and a growing mode $\sim t^{2/3}$.

43] Two types of density perturb; distinction only makes sense before decoupling

A) adiabatic: entropy per comoving volume = const;
 structuring of matter (SB) accompanied by heating (SP)
 Radiation pressure dominates and $P = c_s^2 \rho$ with $c_s = \frac{c}{\sqrt{3}}$
 High c_s responsible for high $M_J \sim \rho_m c^3 \rho_{tot}^{-3/2}$

∇M_J increases with time
 M_J at decoupling was $10^{15} M_\odot \approx$ mass of clusters of galaxies.

B) isothermal: $c_s \sim \sqrt{\frac{BT}{mP}}$ sound velocity $\approx 500 \text{ km/s}$
 400 times less than $c/\sqrt{3}$!!
 $\rightarrow$ once matter and radiation ~~couple~~ decouple,
 M_J drops to the isothermal value

44 fluctuation effects that influence macro structure:

- 1) variation of M_T with time: first increase, then rapid drop.
- 2) horizon mass ($= m$ within horizon distance) is smaller than M_T for adiabatic case (only relevant before decoupling)
- 3) energy diffusion; diffusion of e by Silk damping $\rightarrow$ small scale fluctuations disappeared fast. Silk mass $\sim 10^{12} M_\odot \approx m_{\text{galaxy cluster}}$.

45 Two scenarios:

- A) top-down: clusters of galaxies form first, then separate into individual galaxies. Adiabatic perturb.
- B) bottom-up: small structures (globular clusters, ^{clusters} galaxies) form first, and galaxies follow as assemblies.
Isothermal fluctuations because otherwise Silk damping (also: smaller structures assemble faster).

Two problems:

- a) models achieving structure within reasonable time predict anisotropies $> 10^{-4}$, but in CMB only $< 10^{-5}$ found
- b) deep surveys show hints of structure beyond even superclusters of galaxies.

46 Two dark matter solutions:

- a) d.m. halos can form well before decoupling, so baryons can immediately fall into grav. wells after decoupling $\rightarrow$ top-down possible
- b) d.m. is thus not affected by Silk damping or radiation pressure, so small fluctuations are not erased $\rightarrow$ bottom-up possible in adiabatic, coupled epoch!

47 If d.m. particles have long mean free path, this causes structure on smaller scales; just like photons,

Yes) top-down favored: hot dark matter; nonzero v matters can close the universe.

No) bottom-up still possible: cold d.m. (CDM) scenario. With a cosm. ext., the Λ -CDM scenario predicts large scale structures pretty well.

48] COBE detected also the ~~small~~^{large} scale anisotropies in the CMB. Because of scale-invariance, small scale " also predicted, and detected by WMAP and fitted with the Λ -CDM model. One can decompose them into spherical harmonics.

49] The ~~power~~ power spectrum in terms of angular size / multipole moment - because of the oscillatory density waves - shows acoustic peaks; at decoupling density contrasts are frozen in. Modes that attained extremum at $t = 380,000$ yrs dominate the spectrum: $\frac{1}{k}$ those of sizes $\frac{1}{n} \times \frac{ct}{\sqrt{3}}$ sound travel distance

50] From the CMB spectrum we can determine:

- 1) angular size of object of $\frac{1}{\sqrt{3}} \cdot 380,000$ light yr at $z_{\text{decoupling}}$. This depends on H_0 and Ω , ~~and~~ especially location of first peak!
 $\rightarrow$ determine Ω if H_0 separately known.
- 2) baryon-to-photon ratio (10^{-9}) by inspecting relative amplitudes of the peaks (small peaks affected by Silk damping)
 $\rightarrow$ determine Ω because ρ_{rad} is known from CMB temperature
- 3) dark matter content from the relative amplitudes of successive peaks: d.m. favours odd peaks, but prohibits restoration (even peaks) (contraction)
 $\rightarrow$ determine Ω_{tot} if Ω_{baryons} is known.
- 4) Λ is found by comparing Ω_{dm} and Ω_{baryons} . Also by the integrated Sachs-Wolfe effect: photon falls into gravity well ($\lambda \downarrow$) and ~~after~~ on very large scales when it comes back out: $\lambda \uparrow$ not as much, because of expansion of universe. For nonzero Λ this would have led to flattening of CMB spectrum towards low l .
- 5) overall spectrum yields exponents and of power spectrum of fluctuations

But: these diagnostics are not independent.
e.g. location of 1st peak depends on H_0 ,
and matter density. $\Rightarrow$ full data fits needed
to lift degeneracies, but if so, one can also derive H_0 !

Bonus: primordial He - abundance: He neutralises first $\rightarrow$ decrease in Silk damping!

- 51) Planck and WMAP data do not fully agree. Probably because the CMB contains a lot of noise;
- foreground emission
 - dipole (doppler)
 - mean is large compared to anisotropies

But they agree on the Λ -CDM model and inflation, and anomalies like low quadrupole term, low values for $l \in [20, 30]$ too.

WMAP also detected polarization of CMB, which can occur if e^- density was not isotropic at last (Thomson) scattering.

- 52) Re-ionization: after decoupling, all matter neutral, first stars all very heavy $\rightarrow$ quasars formed $\rightarrow$ universe exposed again to UV-radiation $\rightarrow$ re-ionization.

- 53) ~~Proof~~ Proof that first stars were massive:
- 1) non-zero metallicity of the globular (old) clusters: there must have been a previous, short-lived (and thus massive) generation that polluted them. But: pollution by their own massive stars also possible. Anyway: metal enrichment of galaxies was rapid.
 - 2) γ -ray burst sources (heavy) occur more often at high z . Probably super massive black holes, seeding

- 54) ~~Re~~ Re-ionization occurs when ~~density fluctuations~~ ~~the universe~~ the universe had become locally anisotropic. $\rightarrow$ polarization in CMB stronger than before. WMAP detects maximal polarization power at length scale of $10'$, or $z \approx 14$. (initiated by expansion of polarized CMB until re-ionization) But Gunn-Peterson troughs already disappear at $z = 6$. $\Rightarrow$ the notion of instantaneous re-ionization needs refinement.

55

Gunn - Peterson through:

(13)

neutral H absorbs at Ly- α line. Because of H-clouds at all different z -values on line of sight of observer, one gets a "through" of redshifted Ly- α lines

~~Gunn - Peterson through: after reionisation~~

Ly- α forest: at (partial) reionisation, some (the ionised) H-clouds don't absorb anymore, and one gets a "forest" of Ly- α lines.

56

gravitational lensing: heavy mass between source and observer deflects light. Applications:

- 1) like magnifying glass: observe much more light from distant objects. Very luminous galaxies all have peaks around $100\mu\text{m}$, and redshifting neatly compensates for light dimming due to large distance $\rightarrow$ dimmest $100\mu\text{m}$ objects are lensed galaxies.
- 2) lensing ~~helps~~ helps locating matter in universe
weak lensing: deflections by some object on large # of galaxies must statistically cancel out. When that is observed, the ~~the~~ systematic pattern reveals the unseen deflecting mass.
e.g.: Bullet cluster where dark and baryonic matter are separated.

57

To map the universe, we need ground and space observation

- 1) whole relevant wavelength range: ground only good ~~for~~ for UV-optical-IR, but not for infrared and for radio and higher E.
 - 2) 2D map of the sky: angular resolution depends on wavelength and telescope size, which ~~is~~ is favoured by space and ground observations respectively
 - 3) radial dimension: ~~by~~ observing all z -values: high z means faint objects: high collecting power (ground) vs less diffuse background (space).
- $\Rightarrow$ 2-step approach: space surveys followed up by ground

- 58) surveys from ground ~~are~~ one booming!
- 1) advances in optics combine collecting power with large FOV
 - 2) ICT developments ease data acquisition and storage.

- 59) deep, shallow surveys to probe earlier epochs,
less deep, broad surveys to probe large scale structure
- deep: ~~background~~ X-ray background of first X-ray survey resolved into individual sources: distant galaxies and clusters
 - broad: galaxies up to large scales are not distributed homogeneously: 2D bubbles surrounding less dense regions.

- 60) "Millennium Survey", using the Λ CDM model, confirms filamentary structure, but predicts more oblong galaxies. Explanation: all gas blown away by early, large supernovae $\rightarrow$ ~~the~~ star formation impeded $\rightarrow$ invisible.

- 61) * Space ~~data~~ survey ambitions:
- map matter distribution using weak lensing
 - follow baryonic acoustic oscillations in time ($\Sigma(t)$)
 - bonus: a lot of distant SN's will be revealed, constraining high-order terms in Hubble law $\rightarrow$ better understanding of dark energy component
- * ground surveys might bring meaningful weak-lensing studies by active optics.

- 62) Galaxies treated as ~~as~~ ~~as~~ gas particles, not ~~as~~ entirely correct:
- density is very dilute compared to a ~~gas~~ H-gas.
 - no galaxy is identical to another, unlike atoms.

- 63) Cosmological significance of chemical evolution of galaxies
- 1) evolution from zero metallicity is not linear.
Initial enrichment very rapid: after 10% age, already half the metallic
 - 2) G-dwarf problem: no zero-metallicity stars found yet
→ 1st gen of massive stars OR 1st gen low mass stars more polluted
 - 3) study of relative abundancy trends can determine the evolution of production with time and reveal info about IMF and star-forming intensity
 - 4) identify intruders by deviating elemental ratios.
→ U Centauri is dwarf galaxy swallowed by our system
 - 5) luminosity function of white dwarfs estimates age of galactic disk: $L_b \Rightarrow \text{age} \uparrow$

64) chemical evolution shows evidence for Λ CDM model; ^{bottom-up scenario}
~~early universe contained~~ many merged galaxies like giant elliptical ones
 ↳ during collision, all ISM gas is used for star formation → "starburst" galaxies
 ↳ swallowed a lot of galaxies

65) chicken-or-egg: first black hole or first the starburst? They reinforce each other.
 Black holes speed up galaxy formation, starburst helps accumulating matter.

66) ways to detect high- z galaxies:

- 1) Lyman break (discontinuity): galaxies seen only at ~~high~~ large wavelengths (beyond Ly-limit) have high z .
- 2) red objects
- 3) deep X-ray surveys: hot IGM traces cluster mass.
- 4) lensed features near massive clusters
- 5) ~~parent~~ parent galaxies of γ -ray bursts

- (67) Convergence model based on 3 approaches: (16)
- 1) CMB restricts total energy density (location 1st peak)
 - 2) Hubble diagram (Ia-SN) constrains Λ
 - 3) X-ray output of galaxy clusters traces total (vis + dark) matter.

(68) "dark energy" ~~force~~ (= cause of acceleration)
may refer just to a cosmological Λ .
 Λ 's possible variation with time (less than 6% since decoupling) could indicate another varying scalar field describing vacuum.
→ to know this we need to further study acceleration
→ need more ~~high~~ higher z observations
→ need deep surveys.